**Dynamic Itemset Counting**

**References:**

S. Brin, R. Motwani, J.D. Ullman, S. Tsur, "Dynamic Itemset Counting and Implication Rules for Market Basket Data", *SIGMOD Record*, Volume 6, Number 2: New York, June 1997, pp. 255 - 264.

Su, Yibin, *Dynamic Itemset Counting and Implication Rules for Market Basket Data: Project Final Report, CS831*, April 2000.

**Introduction**

* Alternative to Apriori Itemset Generation
* Itemsets are dynamically added and deleted as transactions are read
* Relies on the fact that for an itemset to be frequent, all of its subsets must also be frequent, so we only examine those itemsets whose subsets are all frequent

Algorithm stops after every *M* transactions to add more itemsets.

* **Train analogy:** There are stations every *M* transactions. The passengers are itemsets. Itemsets can get on at any stop as long as they get off at the same stop in the next pass around the database. Only itemsets on the train are counted when they occur in transactions. At the very beginning we can start counting 1-itemsets, at the first station we can start counting some of the 2-itemsets. At the second station we can start counting 3-itemsets as well as any more 2-itemsets that can be counted and so on.

Itemsets are marked in four different ways as they are counted:

* **Solid box:** DIC Solid Box confirmed frequent itemset - an itemset we have finished counting and exceeds the support threshold *minsupp*
* **Solid circle: DIC Solid Circle** confirmed infrequent itemset - we have finished counting and it is below *minsupp*
* **Dashed box:** DIC Dashed Box suspected frequent itemset - an itemset we are still counting that exceeds *minsupp*
* **Dashed circle:** DIC Dashed Circle suspected infrequent itemset - an itemset we are still counting that is below *minsupp*

**DIC Algorithm**

A Java applet which combines DIC, Apriori and Probability Based Objected Interestingness Measures can be found [here](http://www2.cs.uregina.ca/~dbd/cs831/notes/itemsets/itemsetgenerator.php).

Algorithm:

1. Mark the empty itemset with a solid square. Mark all the 1-itemsets with dashed circles. Leave all other itemsets unmarked.
2. While any dashed itemsets remain:
   1. Read *M* transactions (if we reach the end of the transaction file, continue from the beginning). For each transaction, increment the respective counters for the itemsets that appear in the transaction and are marked with dashes.
   2. If a dashed circle's count exceeds *minsupp*, turn it into a dashed square. If any immediate superset of it has all of its subsets as solid or dashed squares, add a new counter for it and make it a dashed circle.
   3. Once a dashed itemset has been counted through all the transactions, make it solid and stop counting it.

**Itemset lattices:** An itemset lattice contains all of the possible itemsets for a transaction database. Each itemset in the lattice points to all of its supersets. When represented graphically, a itemset lattice can help us to understand the concepts behind the DIC algorithm.

* Example: *minsupp* = 25% and M = 2.

|  |  |  |  |
| --- | --- | --- | --- |
| ***TID*** | ***A*** | ***B*** | ***C*** |
| T1 | 1 | 1 | 0 |
| T2 | 1 | 0 | 0 |
| T3 | 0 | 1 | 1 |
| T4 | 0 | 0 | 0 |

Transaction Database

|  |  |
| --- | --- |
| **Itemset lattice for the above transaction database:**  DIc Lattice 1 | **Itemset lattice before any transactions are read:**  DIC Lattice 2 Counters: A = 0, B = 0, C = 0  Empty itemset is marked with a solid box. All 1-itemsets are marked with dashed circles. |
|  |  |
| **After M transactions are read:**  DIC Lattice 3 Counters: A = 2, B = 1, C = 0, AB = 0  We change A and B to dashed boxes because their counters are greater than minsup (1) and add a counter for AB because both of its subsets are boxes. | **After 2M transactions are read:**  DIC Lattice 4 Counters: A = 2, B = 2, C = 1, AB = 0, AC = 0, BC = 0  C changes to a square because its counter is greater than minsup.A, B and C have been counted all the way through so we stop counting them and make their boxes solid. Add counters for AC and BC because their subsets are all boxes. |
| **After 3M transactions read:**  DIC Lattice 5 Counters: A = 2, B = 2, C = 1, AB = 1, AC = 0, BC = 0  AB has been counted all the way through and its counter satisfies minsup so we change it to a solid box. BC changes to a dashed box. | **After 4M transactions read:**  DIC Lattice 6 Counters: A = 2, B = 2, C = 1, AB = 1, AC = 0, BC = 1  AC and BC are counted all the way through. We do not count ABC because one of its subsets is a circle. There are no dashed itemsets left so the algorithm is done. |

Pseudocode Algorithm:

*SS* =  // solid square (frequent)   
*SC* =  // solid circle (infrequent)   
*DS* =  // dashed square (suspected frequent)   
*DC* = { all 1-itemsets } // dashed circle (suspected infrequent)   
while (DS != 0) or (DC != 0) do begin

read *M* transactions from database into T   
forall transactions t *T*do begin

//increment the respective counters of the itemsets marked with dash   
for each itemset c in *DS* or *DC* do begin

if ( c  t ) then

c.counter++ ;

for each itemset c in *DC*

if ( c.counter  threshold ) then

move c from *DC* to *DS* ;   
if ( any immediate superset sc of c has all of its subsets in *SS* or *DS* )then

add a new itemset sc in *DC* ;

end   
for each itemset c in *DS*

if ( c has been counted through all transactions ) then

move it into *SS* ;

for each itemset c in *DC*

if ( c has been counted through all transactions ) then

move it into *SC* ;

end

end

Answer = { c  SS } ;